BVA⁺ - A BIT VECTORS ALGORITHM FOR ACCELERATING QUERIES IN MULTILEVEL SECURE DATABASES

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Abstract: Much research has been done in the area of multilevel database systems, especially in the security area and accelerating queries. In this paper, we present BVA⁺, which is based on bit vectors to accelerate queries in multilevel secure database systems. As its predecessor (BVA), the BVA⁺ algorithm follows the classic Sea View Model, but it recovers query output from single-level relations in a faster and more space-efficient manner than the previous works performed on this subject. In addition, the BVA⁺ algorithm does not produce spurious or extra tuples, which have always been a major problem in the area of multilevel secure database systems.

1 INTRODUCTION

Much research has been done in the area of multilevel database systems, especially in the security area and accelerating queries (Jajodia, 1991; Sandhu, 1994; Rahal, 2003). One of the earliest attempts to model multilevel relations was the Sea View Model (Lunt, 1990), which represented two algorithms. 1) The decomposition algorithm, which partitioned multilevel relations into single-level relations and stored each single-level relation separately, and 2) The recovery algorithm, which regenerated a multilevel relation from the set of single-level relations. Since multilevel queries would result in applying repeated joins to single-level relations, in addition to the problem of spurious tuples, the Sea View model performed inefficiently. The later works, the DVA algorithm (Perrizo, 1993) and the BVA algorithm (Haraty, 2003), following the Sea View Model, propose faster recovery algorithms and are more space efficient.

In this paper, we follow the widely accepted model for enforcing mandatory access control policies developed by Bell and LaPadula (Bell, 1976) and describe a fast, space efficient, and secure technique for accelerating queries that take place among various single-level relations in a multilevel secure database system. We show that we achieve a significant performance improvement over already published work and produce output data that is consistent.

The rest of this paper is organized as follows: Section 2 provides a brief explanation of multilevel relations and a description of the concept of polyinstantiation. Section 3, presents related work. Section 4 presents the BVA⁺ algorithm and its data structures. Finally, the conclusion is given in section 5.

2 MULTILEVEL RELATIONS AND POLYINSTANTIATION

A multilevel relation (see figure 1) is a relation of the form R (A₁, C₁, ..., Aₙ, Cₙ, TC) where A₁ is an
attribute and \( Ci \) is its classification (or sensitivity level). \( TC \) is the classification of the tuple. \( Ci \) belongs to the domain of classifications for data items. We denote \( Ai \) to be the apparent key of \( R \). The concept of a key is a little bit different in multilevel relations because keys can be duplicated; this is why we refer to them as apparent keys instead of just keys. The reason behind this duplication of keys is polyinstantiation.

<table>
<thead>
<tr>
<th>Name</th>
<th>Objective (obj)</th>
<th>Destination (des)</th>
<th>TC</th>
</tr>
</thead>
<tbody>
<tr>
<td>SHU-1</td>
<td>U</td>
<td>Uranus</td>
<td>U</td>
</tr>
<tr>
<td>APL-9</td>
<td>U</td>
<td>Neptune</td>
<td>C</td>
</tr>
<tr>
<td>RDA-6</td>
<td>U</td>
<td>Pluto</td>
<td>C</td>
</tr>
<tr>
<td>CLB-2</td>
<td>C</td>
<td>Neptune</td>
<td>C</td>
</tr>
<tr>
<td>CLB-2</td>
<td>C</td>
<td>NULL</td>
<td>S</td>
</tr>
</tbody>
</table>

Figure 1. A multilevel relation.

A polyinstantiated tuple is a tuple that exists more than once in a relation with the same apparent key, but with some other attribute values being changed. This is due to the fact that different subjects are authorized to update or view different data. For example, suppose that a subject \( X \) with clearance \( C \) (Confidential) is attempting to write a new value to a data item \( Y \) with sensitivity \( S \) (Secret). The old value in item \( Y \) is not viewable by subject \( X \) but the new value written into \( Y \) by \( X \) is viewable (it has \( X \)'s clearance level which is \( C \)). To preserve the old value of \( Y \), a new tuple is inserted into the relation with same apparent key (and same attribute values except for \( Y \) in this case). Now \( X \) can view the new value inserted into \( Y \) and Secret and Top Secret users will view the two values (the old value with sensitivity \( S \) and the new value with sensitivity \( C \)).

## 3 RELATED WORK

There are many algorithms built for maintaining and recovering multilevel relations from single-level relations. Perhaps the most important of which are the Sea View model, the DVA algorithm, and the BVA algorithm.

### 3.1 The Sea View Model

The Sea View model consists of two algorithms: a decomposition algorithm and a recovery algorithm. The decomposition algorithm divides a multilevel relation \( R \) into a set of single level relations. For every query, an output multilevel relation is reconstructed from the single-level relations using the recovery algorithm. Unfortunately, the recovery algorithm of the Sea View model suffers from the following: a) Creation of spurious tuples in the output (due to polyinstantiation), b) Space inefficiency due to temporary tables, and c) Time inefficiency due to temporary tables and joins, which are two of the most expensive database operations.

### 3.2 The DVA Algorithm

DVA is an algorithm motivated by the recovery algorithm of the Sea View Model based on domain vector accelerators, DVAs, to accelerate the recovery of multilevel relations from single-level relations. DVAs accelerate joins between relations and thus lead to reducing the response time of queries requiring many joins. The DVA algorithm solves the problems of the Sea View Model recovery algorithm; it does not create spurious tuples in the output table and is relatively space and time efficient. It shows improvement especially in environments where queries involve selections on some (one or more) attributes of the multilevel relations. In spite of these facts, this algorithm uses a lot of temporary data structures, some of which can be omitted to improve the algorithm’s space efficiency without negatively affecting its overall performance or its functionality.

### 3.3 The BVA Algorithm

The Bit Vector Algorithm (BVA) is an algorithm also motivated by the recovery algorithm of the Sea View Model to accelerate the recovery of multilevel relations from single-level relations. BVA solves the problems of the Sea View Model recovery algorithm and space and time requirements of the DVA algorithm; it does not create spurious tuples in the output table and is space and time efficient. In spite of these facts, it takes much calculation in finding the temporary storage used to create the output table, and may produce inconsistent data.
4 THE BVA+ ALGORITHM

In this algorithm, we assume that a multilevel relation is decomposed into single level relations using the decomposition algorithm of the Sea View model. The BVA+ algorithm will be applied to recover the multilevel relation from those single level relations. Suppose, we have the multilevel relation in figure 1. This multilevel relation is based on single-level relations as shown in figure 2.

- For every RAix,y excluding base relations create a Mapping Vector Index, MVI.RAix,y, mapping the position of the keys in RAix,y to the position of the keys in RAix. The entries in the MVIs are of the form (pih, pit) where pih, Position In Base relation, is the position of the key in the base relation; and pit, Position In This relation, is the position of the key in this relation.

- Create an Output Keys Vector OKVx (contains all keys with classification x that will appear in the output table) for all x:
  a. As having a number of bits equal to the number of entries in Rkey,x.
  b. Read all relations having an attribute participating in the selection criteria of the query.
  c. Get all entries from those relations satisfying the selection criteria at each level x (at level u we have SHU-1, and APL-9; and at level c we have CLB-2).
  d. For every entry that succeeds, set its position in OKVx to 1. The position of an entry in OKVx can be found by matching the key of this entry to the key in Rkey,x and getting its position in Rkey,x.
     i. OKVu = 110 (the first three keys in Rname,u will appear in output table)
     ii. OKVc = 1 (the first and only key in Rname,u will appear in output table)

- Create a Polyinstantiated Keys Vector, PKVx,y that contains all polyinstantiated keys at level x by subjects at level y, for all x,y such that x<y. For all

![Figure 2. The decomposed single-level relations.](image-url)
attributes \(Ai\) requested in the output of the query (name, obj and des) except for the key (name) do the following:

a. Create \(PKVAi,x,y\) = the ANDing of all \(BV.RAi,x,z\) where \(x < z < y\) for all \(z\)
\[
PK_{\text{obj},u,c} = BV.R_{\text{obj},u,u} \text{ AND } BV.R_{\text{obj},u,c} \\
= 110 \text{ AND } 001 = 000
\]
\[
PK_{\text{obj},u,s} = BV.R_{\text{obj},u,u} \text{ AND } BV.R_{\text{obj},u,c} \\
= 110 \text{ AND } 000 = 000
\]
\[
PK_{\text{obj},c,s} = BV.R_{\text{obj},c,c} \text{ AND } BV.R_{\text{obj},c,s} \\
= 1 \text{ AND } 1 = 1
\]
\[
PK_{\text{des},u,c} = BV.R_{\text{des},u,u} \text{ AND } BV.R_{\text{des},u,c} \\
= 100 \text{ AND } 011 = 000
\]
\[
PK_{\text{des},u,s} = BV.R_{\text{des},u,u} \text{ AND } BV.R_{\text{des},u,c} \\
= 100 \text{ AND } 011 = 000
\]
\[
PK_{\text{des},c,s} = BV.R_{\text{des},c,c} = 1
\]

b. Get \(PKV_{x,y}\) as the ORing of all \(PKVAi,x,y\)
\[
PKV_{u,c} = PK_{\text{obj},u,c} \text{ OR } PK_{\text{des},u,c} = 000
\]
\[
PKV_{u,s} = PK_{\text{obj},u,s} \text{ OR } PK_{\text{des},u,s} = 000
\]
\[
PKV_{c,s} = PK_{\text{obj},c,s} \text{ OR } PK_{\text{des},c,s} = 1
\]

A 1-bit in position \(n\) in any vector \(PKV_{x,y}\) signifies that the \(n\)th entry in \(R_{\text{key},x}\) is polyinstantiated. Therefore, entry 1 in \(R_{\text{name},c}\) that is \(CLB-2\) is polyinstantiated.

\(BVA^+\) differs, in this step, from its predecessor. In order to find if there are any polyinstantiated keys, \(BVA\) creates the Polyinstantiated Key Vector \(PKV\), first by ORing all the Bit Vector \(BV.RAi\)'s, then ANDing the Bit Vectors, again, with the results of the first AND, and finally ends up by ORing all the Polyinstantiated Key Vector \(PKV\)'s (of the attributes) having the same classification. While the \(BVA^+\) algorithm simply ANDs the \(BV.RAi\)'s of each attribute and ORs the resulted \(PKV\)'s (of all the attributes). In this way, \(BVA^+\) simplifies and reduces the calculation, thus making it more efficient both space and time wise.

5. Create \(POKV_{x,y}\) (polyinstantiated output keys vector) as the ANDing of \(PKV_{x,y}\) and \(OKV_{x,x}\)
\[
POKV_{u,c} = \text{OKV}_{u} \text{ AND } PKV_{u,c} \\
= 110 \text{ AND } 000 = 000
\]
\[
POKV_{c,s} = \text{OKV}_{c} \text{ AND } PKV_{c,s} = 1 \text{ AND } 1 = 1
\]

6. Create an Output table, as shown in figure 4, as follows:

a. Having a number of columns equal to the number of fields, \(Ai\), requested in the output of the query (name, obj and des) \(\rightarrow 3\) columns.

b. Scan \(OKV_{x}\) for 1-bit entries (appears in the output). If a 1 bit appears in position \(n\) do the following for all \(Ai\) attributes requested in the output:

   i. If \(Ai\) is the key \((i = 1)\) then get the \(n\)th record from \(R_{Ai,x}\) and store it under \(Ai\) column in output table. This entry has classification \(x\).
   ii. Else, go to the \(n\)th entry in \(BV.R_{Ai,x,z}\) where \(z = x\) initially. If a 1 bit is found in position \(n\) then get the \(p\)'th value of the entry in \(MVI.R_{Ai,x,z}\) that has \(pib = n\). Let \(p = pib\), get the \(p\)'th entry from \(R_{Ai,x,z}\) and store it under \(Ai\) column in output table. This entry has classification \(z\). Else (if 1 bit is not found in position \(n\) of \(BV.R_{Ai,x,z}\) then) increment \(z\) to the next higher level and repeats this step.

   c. Scan \(PKV_{x,y}\) for 1-bit entries (appears in the output and polyinstantiated). If a 1 bit appears in position \(n\) do the following for all \(Ai\) attributes requested in the output:

      i. If \(Ai\) is the key \((Ai = A1)\) then get the \(n\)th record from \(R_{Ai,x}\) and store it under \(Ai\) column in output table. This entry has classification \(x\).
      ii. Else, go to the \(n\)th entry in \(BV.R_{Ai,x,z}\) where \(z = v\) initially. If a 1 bit is found in position \(n\) then get the \(p\)'th value of the entry in \(MVI.R_{Ai,x,z}\) that has \(pib = n\). Let \(p = pib\), get the \(p\)'th entry from \(R_{Ai,x,z}\) and store it under \(Ai\) column in output table. This entry has classification \(z\). Else (if 1 bit is not found in position \(n\) of \(BV.R_{Ai,x,z}\) then) decrement \(z\) to the next lower level and repeats this step. If the \(BV.R_{Ai}\) does not exist then put a null value under the \(Ai\) column in the output table. This entry has classification \(z\).
Part c, is also different from its predecessor. Here, BVA+ requires that if the BV.RAi of any attribute does not exist, (i.e., if it is neither 0 nor 1) a null value under that attribute’s column is inserted. In this way, the output given by the recovery algorithm of BVA+ is proper and consistent with respect to the real database. Thus, BVA+ takes care of null values of the database, which its predecessor – BVA – did not. The null value will have classification z and the algorithm will be repeated for the remaining attributes.

The output table of BVA+ algorithm, after the above stated query, will look like:

<table>
<thead>
<tr>
<th>Name</th>
<th>Objective (obj)</th>
<th>Destination (des)</th>
<th>TC</th>
</tr>
</thead>
<tbody>
<tr>
<td>SHU-1</td>
<td>U</td>
<td>Explore</td>
<td>U</td>
</tr>
<tr>
<td>APL-9</td>
<td>U</td>
<td>Mine</td>
<td>U</td>
</tr>
<tr>
<td>CLB-2</td>
<td>C</td>
<td>Explore</td>
<td>C</td>
</tr>
<tr>
<td>CLB-2</td>
<td>C</td>
<td>Spy</td>
<td>S</td>
</tr>
</tbody>
</table>

5 CONCLUSION

The BVA+ algorithm is an improvement over the Sea View Security Model, and DVA and BVA algorithms. Compared to the first, which was one of the earliest and most important attempts towards multilevel database security, the BVA+ has the following advantages: 1) No spurious tuples in the output table, and 2) No time inefficiency because the BVA+ algorithm does not depend on the use of joins and unions like the Sea View model to create the output table.

When compared with the DVA algorithm, BVA+ is more space and time efficient as it eliminates the following data structures: 1) The Domain Vector Tables (referred to as DVTs in the DVA algorithm) of primary relations, 4) The participation of primary relations in the creation of the Polyinstantiated Domain Vectors (referred to as PDVs in the DVA algorithm), and 5) Select Omit Tables (referred to as SOTs in the DVA algorithm), which are used to produce the Output table.

When compared with the BVA algorithm, BVA+ has the advantages: 1) Reduced calculations in finding one of the temporary storage used to create the output table, and 2) Proper output table, without producing inconsistent data.

REFERENCES


